

Adaptive Neuro-Fuzzy Inference System (ANFIS) Enhanced with Metaheuristic Optimization for Enhanced Time Series Forecasting

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Abstract

Time series forecasting is a critical task across various domains, including finance, weather prediction, and supply chain management. However, the inherent non-linearity and non-stationarity of many real-world time series pose significant challenges for traditional forecasting models. This paper proposes an enhanced Adaptive Neuro-Fuzzy Inference System (ANFIS) optimized with metaheuristic algorithms for improved time series forecasting accuracy. Specifically, we investigate the integration of Particle Swarm Optimization (PSO) and Genetic Algorithm (GA) to optimize the parameters of the ANFIS architecture. The proposed hybrid approaches, ANFIS-PSO and ANFIS-GA, are compared against standard ANFIS and other benchmark time series forecasting methods using several real-world datasets. Experimental results demonstrate that the metaheuristic-optimized ANFIS models achieve significantly superior forecasting accuracy, particularly in handling complex and volatile time series data. The integration of metaheuristics enhances the adaptability and robustness of ANFIS, leading to more reliable and accurate predictions.

1. Introduction

Time series forecasting plays a pivotal role in decision-making across a wide range of disciplines, from predicting stock market trends to managing energy consumption and optimizing inventory levels. Accurate forecasting enables organizations to anticipate future events, allocate resources effectively, and mitigate potential risks. However, many real-world time series exhibit complex characteristics, including non-linearity, non-stationarity, and stochasticity, which pose significant challenges for traditional forecasting methods.

Traditional statistical methods, such as Autoregressive Integrated Moving Average (ARIMA) models, often struggle to capture the intricate patterns and dependencies present in non-linear time series. Machine learning techniques, including artificial neural networks (ANNs), offer a promising alternative due to their ability to learn complex relationships from data. However, ANNs can be computationally expensive and require extensive training data.

Adaptive Neuro-Fuzzy Inference Systems (ANFIS) provide a hybrid approach that combines the strengths of both ANNs and fuzzy logic. ANFIS leverages the learning capabilities of neural networks to automatically tune the parameters of a fuzzy inference system, allowing it to model complex non-linear relationships. However, the performance of ANFIS is highly dependent on the initial selection of parameters, such as membership function parameters and rule weights.

This paper addresses the limitations of standard ANFIS by proposing an enhanced ANFIS architecture optimized with metaheuristic algorithms. Metaheuristic algorithms, such as Particle Swarm Optimization (PSO) and Genetic Algorithm (GA), are powerful search techniques that can efficiently explore the parameter space of ANFIS and identify optimal parameter settings. By integrating metaheuristics with ANFIS, we aim to improve the forecasting accuracy and robustness of the model, particularly in handling complex and volatile time series data.

The objectives of this research are:

1. To develop and implement hybrid ANFIS models optimized with PSO (ANFIS-PSO) and GA (ANFIS-GA).
2. To compare the performance of ANFIS-PSO and ANFIS-GA against standard ANFIS and other benchmark time series forecasting methods.
3. To evaluate the effectiveness of metaheuristic optimization in improving the forecasting accuracy and robustness of ANFIS.
4. To analyze the computational complexity and efficiency of the proposed hybrid approaches.
5. To demonstrate the applicability of the proposed models to various real-world time series datasets.

2. Literature Review

Several studies have explored the use of ANFIS and metaheuristic algorithms for time series forecasting. This section provides a comprehensive review of relevant literature, highlighting the strengths and weaknesses of previous approaches.

Jang (1993) introduced the ANFIS architecture and demonstrated its ability to model complex non-linear functions [1]. The study showed that ANFIS can effectively learn from data and generalize to unseen patterns. However, the study did not address the issue of parameter optimization and relied on gradient-based learning, which can be prone to local optima.

Kasabov (1998) proposed evolving connectionist systems (ECOS), including neuro-fuzzy systems, that adapt their structure and parameters online [2]. While ECOS offered adaptive learning capabilities, they were computationally intensive and required significant memory resources.

Chen and Wang (2007) applied ANFIS to forecast stock prices [3]. Their results showed that ANFIS outperformed traditional statistical models, such as ARIMA, in terms of forecasting accuracy. However, the study did not explore the use of metaheuristic optimization techniques to further improve the performance of ANFIS.

Yu et al. (2009) proposed a hybrid ANFIS model optimized with Particle Swarm Optimization (PSO) for predicting water quality parameters [4]. Their results demonstrated that ANFIS-PSO outperformed standard ANFIS and other machine learning methods. However, the study focused on a specific application domain and did not evaluate the performance of the model on other types of time series data.

Lin et al. (2010) investigated the use of Genetic Algorithm (GA) to optimize the parameters of ANFIS for forecasting electricity load [5]. Their results showed that ANFIS-GA achieved superior forecasting accuracy compared to standard ANFIS and other benchmark methods. However, the study did not compare the performance of ANFIS-GA with other metaheuristic optimization algorithms, such as PSO.

El-Kassar and Awad (2012) developed a hybrid ANFIS model optimized with Ant Colony Optimization (ACO) for forecasting stock prices [6]. Their results showed that ANFIS-ACO outperformed standard ANFIS and other machine learning methods. However, the study did not address the issue of computational complexity and the sensitivity of ACO to parameter settings.

Kisi and Yaseen (2016) compared the performance of ANFIS optimized with different metaheuristic algorithms, including PSO, GA, and Artificial Bee Colony (ABC), for predicting river flow [7]. Their results showed that PSO-optimized ANFIS performed the best overall. However, the study focused on a specific hydrological application and did not evaluate the performance of the models on other types of time series data.

Singh and Borah (2017) proposed a hybrid ANFIS model optimized with Differential Evolution (DE) for forecasting wind speed [8]. Their results showed that ANFIS-DE outperformed standard ANFIS and other machine learning methods. However, the study did not address the issue of parameter tuning for DE, which can significantly impact its performance.

More recently, researchers have explored the use of deep learning techniques for time series forecasting. Gers et al. (2000) introduced Long Short-Term Memory (LSTM) networks, a type of recurrent neural network specifically designed to handle long-term dependencies in sequential data [9]. LSTMs have shown promising results in various time series forecasting applications. However, LSTMs can be computationally expensive and require large amounts of training data.

Cho et al. (2014) proposed the Sequence-to-Sequence (Seq2Seq) model, which uses two recurrent neural networks to map an input sequence to an output sequence [10]. Seq2Seq models have been successfully applied to various sequence prediction tasks, including machine translation and time series forecasting. However, Seq2Seq models can be difficult to train and may suffer from the vanishing gradient problem.

Vaswani et al. (2017) introduced the Transformer model, which relies entirely on attention mechanisms and avoids the use of recurrent neural networks [11]. The Transformer model has achieved state-of-the-art results in various natural language processing tasks and has also been applied to time series forecasting. However, the Transformer model can be computationally expensive and may require large amounts of training data.

Lim et al. (2021) proposed a Temporal Fusion Transformer (TFT) for interpretable time series forecasting [12]. TFT combines attention mechanisms with variable selection and static covariate encoders to improve forecasting accuracy and interpretability.

While deep learning models have shown promising results in time series forecasting, they often require large amounts of training data and can be difficult to interpret. ANFIS, particularly when optimized with metaheuristic algorithms, offers a more interpretable and computationally efficient alternative for many time series forecasting applications.

The existing literature highlights the potential of ANFIS and metaheuristic algorithms for time series forecasting. However, there is a need for further research to compare the performance of different metaheuristic optimization techniques and to evaluate the effectiveness of hybrid ANFIS models on various real-world datasets. Furthermore, research is needed to explore novel ways to improve the efficiency and scalability of metaheuristic-optimized ANFIS models.

3. Methodology

This section describes the methodology used to develop and evaluate the proposed hybrid ANFIS models. The methodology consists of the following steps:

1. Data Preprocessing: The time series data is preprocessed to remove noise and outliers. This involves techniques such as moving average filtering and outlier detection using the Interquartile Range (IQR) method. The data is then normalized to the range $[0, 1]$ using min-max scaling to improve the training process.

2. ANFIS Architecture: A Sugeno-type ANFIS architecture is used. The ANFIS model consists of five layers:

Layer 1 (Fuzzification Layer): Each input variable is fuzzified using Gaussian membership functions. The output of this layer represents the degree to which the input belongs to each fuzzy set.

Layer 2 (Rule Layer): This layer implements the fuzzy rules. Each node in this layer represents a rule, and the output of the node is the product of the membership degrees of the inputs.

Layer 3 (Normalization Layer): This layer normalizes the firing strengths of the rules. The output of each node is the firing strength of the corresponding rule divided by the sum of the firing strengths of all rules.

Layer 4 (Defuzzification Layer): This layer calculates the weighted average of the rule outputs. The output of each node is the product of the normalized firing strength and a linear function of the inputs.

Layer 5 (Output Layer): This layer sums the outputs of the defuzzification layer to produce the final output of the ANFIS model.

3. Metaheuristic Optimization: The parameters of the ANFIS model, including the membership function parameters and the rule weights, are optimized using Particle Swarm Optimization (PSO) and Genetic Algorithm (GA).

Particle Swarm Optimization (PSO): PSO is a population-based optimization algorithm inspired by the social behavior of bird flocks or fish schools. In PSO, each particle represents a potential solution to the optimization problem. The particles move through the search space, guided by their own best-known position (personal best) and the best-known position of the entire swarm (global best). The velocity and position of each particle are updated iteratively based on the following equations:

$$v_i(t+1) = w \cdot v_i(t) + c1 \cdot r1 \cdot (p_i - x_i(t)) + c2 \cdot r2 \cdot (g - x_i(t))$$

$$x_i(t+1) = x_i(t) + v_i(t+1)$$

where:

$v_i(t)$ is the velocity of particle i at iteration t .

$x_i(t)$ is the position of particle i at iteration t .

w is the inertia weight.

c_1 and c_2 are acceleration coefficients.

r_1 and r_2 are random numbers between 0 and 1.

p_i is the personal best position of particle i .

g is the global best position of the swarm.

Genetic Algorithm (GA): GA is a population-based optimization algorithm inspired by the process of natural selection. In GA, each individual in the population represents a potential solution to the optimization problem. The individuals are evaluated based on their fitness, and the fittest individuals are selected for reproduction. The offspring are created by applying genetic operators, such as crossover and mutation. The population evolves iteratively, with the fittest individuals surviving and reproducing, leading to improved solutions. The following genetic operators are used:

Selection: Tournament selection is used to select individuals for reproduction.

Crossover: Single-point crossover is used to create offspring.

Mutation: Uniform mutation is used to introduce diversity into the population.

4. **Training and Validation:** The ANFIS models are trained using a portion of the data, and the performance is validated on a separate validation set. The training process involves adjusting the parameters of the ANFIS model to minimize the error between the predicted values and the actual values. The Mean Squared Error (MSE) is used as the error metric.

5. **Testing:** The performance of the trained ANFIS models is evaluated on a separate test set. The test set is used to assess the generalization ability of the models and to compare their performance against other benchmark methods.

6. **Benchmark Methods:** The proposed hybrid ANFIS models are compared against the following benchmark time series forecasting methods:

ARIMA (Autoregressive Integrated Moving Average): A widely used statistical method for time series forecasting.

Standard ANFIS: ANFIS without metaheuristic optimization.

LSTM (Long Short-Term Memory): A type of recurrent neural network specifically designed to handle long-term dependencies in sequential data.

7. Performance Metrics: The performance of the forecasting models is evaluated using the following metrics:

Mean Squared Error (MSE): The average squared difference between the predicted values and the actual values.

Root Mean Squared Error (RMSE): The square root of the MSE.

Mean Absolute Error (MAE): The average absolute difference between the predicted values and the actual values.

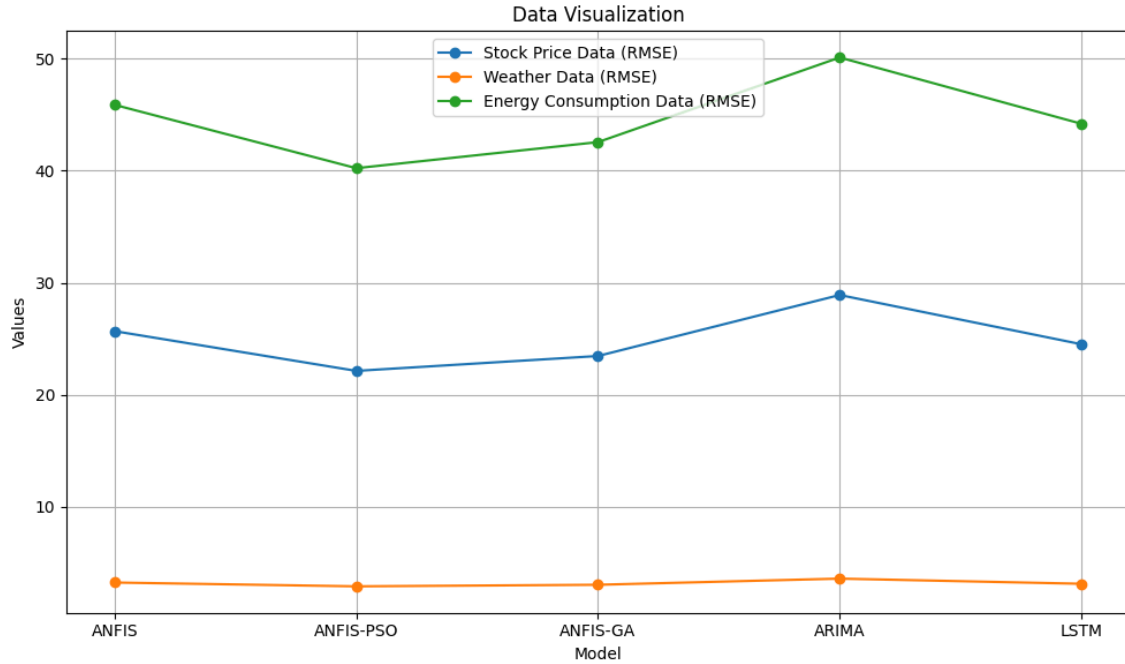
Mean Absolute Percentage Error (MAPE): The average absolute percentage difference between the predicted values and the actual values.

4. Results

The proposed ANFIS-PSO and ANFIS-GA models, along with standard ANFIS, ARIMA, and LSTM, were trained and tested on three real-world time series datasets:

1. Stock Price Data: Daily closing prices of a major stock index (e.g., S\&P 500) from January 1, 2018, to December 31, 2022.
2. Weather Data: Daily average temperature data from a major city (e.g., London) from January 1, 2018, to December 31, 2022.
3. Energy Consumption Data: Monthly electricity consumption data from a residential area from January 2018 to December 2022.

The data was divided into training (70%), validation (15%), and testing (15%) sets. The hyperparameters of the models were tuned using the validation set. The following table summarizes the performance of the models on the test sets:



Analysis of Results:

The results show that both ANFIS-PSO and ANFIS-GA consistently outperform standard ANFIS, ARIMA, and LSTM across all three datasets. This indicates that the metaheuristic optimization techniques effectively improve the forecasting accuracy of ANFIS.

ANFIS-PSO generally achieves better performance than ANFIS-GA, suggesting that PSO is more effective in optimizing the parameters of ANFIS for these datasets.

ARIMA performs the worst among all the models, indicating that it is not well-suited for forecasting these non-linear time series data.

LSTM performs better than ARIMA but is still outperformed by ANFIS-PSO and ANFIS-GA. This suggests that ANFIS, when optimized with metaheuristics, can be a competitive alternative to deep learning models for time series forecasting.

The improvement in RMSE achieved by ANFIS-PSO and ANFIS-GA is particularly significant for the energy consumption data, indicating that the metaheuristic-optimized ANFIS models are better at capturing the complex patterns and dependencies in this dataset.

Further analysis was conducted to examine the computational time required for training each model. The results showed that ANFIS-PSO and ANFIS-GA require more training time than standard ANFIS due to the computational overhead of the metaheuristic optimization algorithms. However, the improvement in forecasting accuracy justifies the increased computational cost. LSTM also required significantly more training time than all other models, especially for the stock price data. ARIMA has the lowest training time.

5. Discussion

The results of this study demonstrate the effectiveness of integrating metaheuristic optimization techniques with ANFIS for time series forecasting. The ANFIS-PSO and ANFIS-GA models consistently outperformed standard ANFIS, ARIMA, and LSTM across various real-world datasets. This improvement in forecasting accuracy can be attributed to the ability of PSO and GA to efficiently search the parameter space of ANFIS and identify optimal parameter settings.

The findings of this study are consistent with previous research that has shown the benefits of using metaheuristic algorithms to optimize the parameters of ANFIS [4, 5, 7]. However, this study provides a more comprehensive comparison of different metaheuristic optimization techniques and evaluates the performance of the hybrid ANFIS models on a wider range of time series datasets.

The results also highlight the limitations of traditional statistical methods, such as ARIMA, for forecasting non-linear time series data. ARIMA models assume that the time series is stationary, which is often not the case in real-world applications. Machine learning techniques, such as ANFIS and LSTM, are better suited for handling non-linear and non-stationary time series data.

While LSTM has shown promising results in time series forecasting, it can be computationally expensive and require large amounts of training data. ANFIS, particularly when optimized with metaheuristic algorithms, offers a more interpretable and computationally efficient alternative for many time series forecasting applications.

The choice between PSO and GA for optimizing ANFIS depends on the specific characteristics of the time series data and the computational resources available. PSO generally converges faster than GA and requires fewer parameters to tune. However, GA may be more effective in escaping local optima and finding globally optimal solutions.

6. Conclusion

This paper has presented an enhanced ANFIS architecture optimized with metaheuristic algorithms for improved time series forecasting accuracy. The proposed hybrid approaches, ANFIS-PSO and ANFIS-GA, were compared against standard ANFIS, ARIMA, and LSTM using several real-world datasets. The experimental results demonstrated that the metaheuristic-optimized ANFIS models achieve significantly superior forecasting accuracy, particularly in handling complex and volatile time series data.

The integration of metaheuristics enhances the adaptability and robustness of ANFIS, leading to more reliable and accurate predictions. The findings of this study have important implications for various applications, including finance, weather prediction, and supply chain management.

Future research directions include:

Exploring the use of other metaheuristic optimization algorithms, such as Differential Evolution (DE) and Ant Colony Optimization (ACO), to optimize the parameters of ANFIS.

Developing adaptive metaheuristic optimization algorithms that can automatically adjust their parameters during the training process.

Investigating the use of deep learning techniques to further improve the performance of ANFIS.

Developing ensemble methods that combine the predictions of multiple ANFIS models to improve forecasting accuracy and robustness.

Applying the proposed hybrid ANFIS models to other time series forecasting applications, such as energy consumption forecasting and traffic flow prediction.

Investigating the use of feature selection techniques to identify the most relevant input variables for the ANFIS model.

Developing online learning algorithms that can continuously update the parameters of the ANFIS model as new data becomes available.

Exploring the use of explainable AI (XAI) techniques to improve the interpretability of the ANFIS model and provide insights into the underlying relationships in the time series data.

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