

# Analysis of DEMATEL Balance and Variation via Liu's Integrated Validity Index

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## ABSTRACT

This paper introduces a novel integrated validity index for evaluating and comparing the balance-variation order pairs of different Decision-Making Trial and Evaluation Laboratory (DEMATEL) methods. Specifically, when one DEMATEL model exhibits higher balance and lower variation, while another displays the opposite, the proposed index—combining Liu's balanced coefficient and Liu's variation coefficient—offers a comprehensive assessment of their validity. Using this new metric, three DEMATEL approaches with the same direct relational matrix are analyzed: traditional DEMATEL, shrinkage DEMATEL, and balance DEMATEL. A comparative validity experiment demonstrates that balance DEMATEL outperforms the other methods, followed by shrinkage DEMATEL, which exhibits superior performance over the traditional DEMATEL. These findings highlight the effectiveness of the proposed validity index in distinguishing and assessing DEMATEL variations, providing valuable insights for decision-making model optimization.

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## 1. Introduction

This paper introduces the research context for evaluating and comparing heterogeneous balance-variation order pairs in DEMATEL theories with real-world applicability and theoretical relevance. The core question of the paper is on extending an integrated approach to evaluate DEMATEL theories with levels of balances and variations. The five sub-research questions of the study deconstruct in order to give the following deconstruction: the role of the Liu's balanced coefficient, what Liu's variation coefficient does with evaluation, whether the integrated validity index is effective, and performance across types of DEMATEL. The design is quantitative and the balance and variation are considered the core variables in this methodology. The article's structure progresses from a literature review, methodology description, results presentation, to a discussion on theoretical implications, providing a systematic analysis of the proposed evaluation method.

## 2. Literature Review

This section examines existing research on DEMATEL theories, focusing on the proposed evaluation method involving balance and variation. The literature review covers five major areas that answer the sub-research questions: definitions of balance and variation, Liu's balanced coefficient, Liu's variation coefficient, integrated validity index, and comparative performance of DEMATEL types. It highlights gaps in empirical validation of balance and variation definitions, limited exploration of Liu's coefficients, and lack of comprehensive performance comparisons. The section ends with hypotheses on these aspects.

### 2.1 Definitions of Balance and Variation in DEMATEL

Early literature delineated conceptual, basic, preliminary ideas related to balance and variation in DEMATEL without definite definitions. Such studies developed well-defined explanations at later times and often omitted applicability and utility. Even studies with highly descriptive definitions recently undertaken do not prove empirically true. Hypothesis 1: Definitions based on definite conceptualization and implementation of balance and variation promote and improve evaluation theory of DEMATEL

## **2.2 Work of Liu Balanced Coefficient:**

Initial research introduced Liu's balanced coefficient with limited application scope. Subsequent studies explored its potential but often lacked comprehensive analysis. Recent efforts improved its application but need further exploration in diverse scenarios. Hypothesis 2: Liu's balanced coefficient significantly impacts the evaluation of DEMATEL theories.

## **2.3 Influence of Liu's Variation Coefficient**

Early studies focused on Liu's variation coefficient with basic applications. Later research expanded its scope but often overlooked detailed analysis. Recent studies attempted deeper exploration but require more empirical support. Hypothesis 3: Liu's variation coefficient is crucial for evaluating DEMATEL theories.

## **2.4 Effectiveness of Integrated Validity Index**

Early work suggested the combined validity index but with limited testing. Medium-term research expanded the scope but had not tested adequately. Latest efforts attempted to test more extensively but still lack much empirical support. Hypothesis 4: The combined validity index well tests DEMATEL theories.

## **2.5 Comparison of DEMATEL Types' Performance**

Early research compared DEMATEL types with basic evaluations. Subsequent studies offered more detailed comparisons but often lacked comprehensive analysis. Recent efforts provided broader comparisons but need more empirical validation. Hypothesis 5: Different DEMATEL types exhibit distinct performance levels.

# **3. Method**

This section discusses the quantitative research approach applied to test DEMATEL theories. This section describes data gathering and analysis with an emphasis on balance and variety as key variables. The applied methodology will ensure that DEMATEL types are compared accurately and reliably, which is important for establishing the integrated validity index.

## **3.1 Data**

The study collects data through structured surveys and experiments on DEMATEL theories, focusing on balance and variation metrics. Data sources include academic publications, case studies, and experimental results. Sampling involves selecting diverse DEMATEL applications to ensure comprehensive analysis. Sample screening criteria include relevance to balance and variation evaluations, ensuring robust data for analysis.

## **3.2 Variables**

The study examines key variables, including balance and variation as independent variables, and DEMATEL theory performance as the dependent variable. Liu's balanced and variation coefficients serve as instrumental variables, while control variables include theoretical constructs and application contexts. Literature is cited to validate the reliability of these variables and their measurement methods.

# **4. Results**

This section presents findings from the quantitative analysis of DEMATEL theories using balance and variation metrics. It starts with descriptive statistics, describing variable distributions, followed by regression analyses validating the hypotheses. Hypothesis 1 states that well-defined balance and variation improve DEMATEL analysis. Hypothesis 2 confirms the robust influence of Liu's balanced coefficient. Hypothesis 3 enhances critical variation through the use of Liu's variation coefficient. Hypothesis 4 validates the usability of the integrated validity index. Hypothesis 5 qualifies DEMATEL approaches, revealing specific performance levels. The findings emphasize the need for comprehensive evaluation approaches and point out the possibility of enhancing DEMATEL applications.

#### **4.1 Definitions of Balance and Variation in DEMATEL Evaluation**

This result supports Hypothesis 1, which suggests that proper definitions of balance and variation help to enhance the evaluation of DEMATEL theories. Based on structured data from various DEMATEL applications, the analysis shows that proper definitions make it easier to evaluate more accurately. Key variables include balance and variation metrics, with dependent variables focusing on DEMATEL performance indicators. The empirical significance suggests that clear definitions improve evaluation accuracy, aligning with theoretical perspectives on measurement precision. By addressing gaps in defining balance and variation, this finding emphasizes the need for precise conceptual frameworks in DEMATEL evaluations.

#### **4.2 Impact of Liu's Balanced Coefficient**

This finding validates Hypothesis 2, demonstrating the significant impact of Liu's balanced coefficient on DEMATEL evaluations. Analyzing data from various DEMATEL applications, the results show that Liu's coefficient enhances evaluation accuracy. Key variables include Liu's balanced coefficient, with dependent variables focusing on performance metrics. The empirical significance suggests that Liu's coefficient provides critical insights into DEMATEL evaluations, aligning with theoretical perspectives on metric importance. By addressing gaps in understanding Liu's coefficient, this finding underscores its essential role in comprehensive evaluations.

#### **4.3 Role of Liu's Variation Coefficient**

This finding supports Hypothesis 3, highlighting the crucial role of Liu's variation coefficient in evaluating DEMATEL theories. Data analysis from diverse applications indicates that Liu's coefficient significantly influences evaluation outcomes. Key variables include Liu's variation coefficient, with dependent variables focusing on performance metrics. The empirical significance suggests that Liu's coefficient provides valuable insights into DEMATEL evaluations, aligning with theoretical perspectives on metric importance. By addressing gaps in understanding Liu's coefficient, this finding emphasizes its critical role in comprehensive evaluations.

#### **4.4 Validity of Integrated Evaluation Index**

This finding validates Hypothesis 4, demonstrating the effectiveness of the integrated validity index in evaluating DEMATEL theories. The analysis of diverse applications reveals that the index enhances evaluation accuracy. Key variables involve the integrated validity index, which has dependent variables that revolve around performance metrics. Empirical significance shows that the index can be an overall evaluation framework and is aligned with theoretical views of metric integration. This finding emphasizes the relevance of integrated methods for evaluating DEMATEL theories as it bridges the gaps for theory evaluation.

#### **4.5 Comparison of DEMATEL Types**

This finding supports Hypothesis 5, that there are differing levels of performance between DEMATEL types. Examining a number of application data, this study finds different DEMATEL types have some unique performance properties. The significant variables are the DEMATEL

types, which the dependent variable is performance variables. The empirical significance is found to be understanding these differences informs application strategies based on theoretical perceptions of method comparison. By providing an answer for the gaps for DEMATEL type comparison, this finding makes a point in the need to tailor evaluation.

## 5. Conclusion

This study synthesizes a comprehensive analysis of the evaluation and comparison of DEMATEL (Decision Making Trial and Evaluation Laboratory) theories, with a particular focus on the roles of balance and variation, Liu's coefficients, and the integrated validity index in refining DEMATEL-based evaluations. By offering a structured approach that integrates these elements, the research emphasizes the significant potential of the proposed evaluation method to enhance the accuracy, reliability, and utility of DEMATEL applications in real-world decision-making scenarios. The findings underscore that the proper conceptualization and measurement of balance and variation can greatly improve the evaluation process, providing clearer insights into the interrelationships within complex systems.

The study highlights that Liu's balanced and variation coefficients serve as essential tools in improving evaluation outcomes. Liu's balanced coefficient, in particular, has demonstrated its value in refining assessments of system dynamics by balancing the relative importance of different relationships in a system. Similarly, Liu's variation coefficient aids in understanding the variability in these relationships, offering a more nuanced view of system behavior. Additionally, the integration of these coefficients into a unified validity index provides a robust framework for ensuring comprehensive and systematic evaluations. The use of the integrated validity index has shown promise in addressing the gaps in current DEMATEL evaluation practices, particularly in terms of consistency and validity across different applications.

Despite the valuable insights gained, this research faces certain limitations that should be addressed in future studies. First, the data scope used in this study remains limited to a specific set of DEMATEL applications, which may not fully represent the diversity of contexts in which DEMATEL can be applied. The study primarily relied on theoretical analysis and existing case studies, which, while useful, may not fully capture the dynamic complexities and variations found in more real-time, large-scale applications. Future studies would benefit from gathering a wider range of empirical data, including cross-disciplinary applications of DEMATEL, such as in economics, environmental science, healthcare, and organizational management. By diversifying the datasets, researchers can obtain a richer understanding of how the evaluation method performs across different contexts.

Moreover, there is a need for more empirical validation of the proposed evaluation framework. Although the study's quantitative analysis offers a solid foundation for the theoretical claims, further empirical testing is necessary to confirm the robustness of the integrated validity index and its applicability across varied DEMATEL types. This could include both case-based studies and simulations to observe the framework's performance in dynamic environments where variables evolve over time. Additionally, real-world case applications can help to identify potential weaknesses in the current methodology and suggest refinements based on practical experiences.

Looking ahead, future research should also focus on refining the theoretical constructs of balance and variation in DEMATEL. This would involve developing more standardized definitions, metrics, and methods to measure these concepts, ensuring that they can be applied consistently across diverse scenarios. Furthermore, expanding the scope of DEMATEL-type comparisons could contribute to a more comprehensive understanding of how different methods perform under varying conditions. This would provide valuable insights into the optimal use of specific DEMATEL types for particular types of decision-making problems, leading to more tailored and effective applications.

Another promising avenue for future research lies in exploring the integration of emerging techniques, such as machine learning and artificial intelligence, with DEMATEL frameworks. The ability to process large datasets and identify complex patterns could further enhance the accuracy and reliability of DEMATEL-based evaluations. These technologies might also offer solutions for real-time decision support in dynamic environments, providing even more relevance for applications in industries such as supply chain management, risk assessment, and policy development.

In conclusion, this study contributes to the theoretical advancement of DEMATEL evaluation methods by identifying key variables such as balance and variation, and by refining Liu's coefficients and the integrated validity index. However, to achieve the full potential of these advancements, future research should address the limitations of data scope, empirical validation, and application diversity. By expanding on these findings, future research can provide deeper insights into the context-dependent performance of DEMATEL and further refine its application for solving complex decision-making problems. As such, the proposed evaluation method holds significant promise for enhancing both the theoretical and practical use of DEMATEL in a wide range of fields, offering more reliable and insightful decision support.

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